The fundamental physical constants

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The Committee on Data for Science and Technology was established in 1966 as an interdisciplinary committee of the International Council of Scientific Unions (now the International Council of Science). Three years later, CODATA created the task group on fundamental constants to periodically provide the scientific and technological communities with a self-consistent set of internationally recommended values for the basic constants and conversion factors of physics and chemistry. Under the auspices of the task group, we have completed a new least-squares adjustment of those values--termed the 2002 adjustment--that takes into account all relevant data available through 31 December 2002. The accompanying tables give the 2002 CODATA recommended values resulting from that adjustment, except for some specialized x-ray-related quantities and various natural and atomic units.

The complete 2002 CODATA set of more than 300 recommended values, together with a detailed description of the data and their analysis, is given in reference 1. All of the values, as well as the correlation coefficients between any two constants, are available online in a searchable database provided by NIST's fundamental constants data center. The internet address is http://physics.nist.gov/constants.

The 2002 CODATA set replaces its immediate predecessor, which resulted from the 1998 adjustment,² also carried out under the auspices of the task group. Only four years have elapsed between the 31 December 1998 and 31 December 2002 closing dates of the two adjustments (12 years separated the 1998 adjustment and its predecessor), but a number of advances in experiment and theory have led to improvements in our knowledge of the values of the constants.

The new information includes measurements of the Newtonian constant of gravitation G; improved experimental values of the relative atomic masses of helium-4, oxygen-16, and cesium-133 (carbon-12 has a relative atomic mass of exactly 12, by definition); a more accurate value of the $1S_{1/2}2S_{1/2}$ transition frequency in hydrogen; a new result for the bound-state root-mean-square (rms) charge radius of the proton $R_{\rm p}$; and highly accurate measurements related to the bound-state g-factor of the electron in the hydrogenic ions $^{12}C^{5+}$ and $^{16}O^{7+}$. Additional experimental refinements include a new, quite accurate measurement of the muon magnetic moment anomaly a_{μ} ; an accurate value, obtained from the atomic recoil frequency shift of photons absorbed and emitted by Cs atoms, for the quotient $h/m(^{133}Cs)$, where h is the Planck constant and $m(^{133}Cs)$ is the mass of the ^{133}Cs atom; a result for the molar volume of silicon $V_{\rm m}(Si)$; and new experimental findings concerning previous measurements of the $\{220\}$ lattice spacing of particular Si crystals.

299 792 458 4#×10⁻⁷ =12.566 370 614 . . .×10⁻⁷ 8.854 187 817 . . .×10⁻¹² 376,730 313 461 . . 6.6742(10)×10⁻¹³ 6.7087(10)×10⁻²⁴ 6.626 0693(11)×10⁻²⁴



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Theorists have developed improved expressions for the hydrogen and deuterium energy levels, the electron and muon magnetic moment anomalies a_e and a_μ , the ground-state hyperfine splitting of muonium (that is, the μ^+e^- "atom"), and the electron bound-state g-factor in hydrogenic ions.

CONSEQUENCES OF NEW RESULTS

The new information available to the task group led to significant changes in both the values and the uncertainties of many of the fundamental constants. A few highlights follow.

- The new results for G agreed sufficiently well among themselves to convince the task group that an earlier, highly discrepant but credible result need no longer be considered in determining the recommended value. That decision led to a new recommended value of G with a relative standard uncertainty (that is, relative estimated standard deviation) $u_r = 1.5 \times 10^{-4}$. The new u_r is a factor of 10 smaller than that of the 1998 recommended value.
- Accurate measurements of the frequency ratios $f_s(^{12}C^{5+})/f_c(^{12}C^{5+})$ and $f_s(^{16}O^{7+})/f_c(^{16}O^{7+})$, together with the theoretical expression for the boundstate g-factor of the electron in each ion, have yielded values for the relative atomic mass of the electron A_e(e) and the electron-to-proton mass ratio m_a/m_B with relative uncertainties of about 5 × 10⁻¹⁰. (In the expressions for the frequency ratios, f is the precession, or "spin-flip," frequency of the electron in the ground state of the indicated hydrogenic ion in an applied magnetic flux density, and f is the cyclotron frequency of the ion in the same flux density.) Compared to the 1998 uncertainties, the new uncertainties represent a reduction by more than a factor of four.
- The new result for V_m(Si) is credible, but inconsistent with four credible measurements of other quantities. Thus, one or more of the five results has a problem. We present some details below about the discrepancy and how we dealt with it.
- The 1998 adjustment included input from three combined x-ray and optical-interferometer determinations of the {220} lattice spacing

- of particular Si crystals. Subsequently, it was discovered that two of those three experiments appeared to have problems, so the data from those experiments were not included in the 2002 adjustment. Removing these data eliminates the scatter in the fine-structure-constant (α) values implied by the accurate x-ray measurement of h/m_n, where m_n is the neutron mass. Moreover, the value of α inferred from h/m_n now agrees well with values of α from other sources.
- An error was discovered in the eighth-order coefficient A₁⁽⁸⁾ in the theoretical expression for the electron magnetic moment anomaly a_e(th). That discovery has led to a fractional increase of 5.7 × 10⁻⁹ in the value for α implied by the experimental result for a_e, about 1.5 times the relative uncertainty of the 1998 a_e value of α. Other experiments also yield values for α. In particular, the new result for h/m(1³³Cs) has yielded a reduction of the uncertainty of the recommended value of α from u_r 3.7 × 10⁻⁹ in 1998 to u_e 3.3 × 10⁻⁹.
- The significant advances in the theory of hydrogen and deuterium energy levels and the improved value of R_p have eliminated a systematic deviation between theory and experiment observed in the 1998 adjustment. As a result, the CODATA set now includes recommended values for R_p and the bound-state rms charge radius of the deuteron R_d.

DATA ANALYSIS

The 2002 adjustment is similar to the 1998 adjustment in many key respects. First, we treat all of the input data on an essentially equal footing, regardless of their uncertainties. Doing so allows us to properly consider all components of uncertainty and all significant correlations among the data. It also eliminates any arbitrary division of the data into different categories--such divisions generally occurred in adjustments before that of 1998.

Second, we used the standard least-squares algorithm to analyze the data rather than an extended algorithm that tries to take into account the "uncertainty of the uncertainty" assigned to an input datum. An extended algorithm was applied as part of the 1986 adjustment,³ but the complexity of

the measurements and calculations in the field of fundamental constants makes it difficult enough to evaluate uncertainties in a meaningful way, let alone the uncertainties of those uncertainties.

Third, we reprised an innovation from the 1998 adjustment to properly take into account the uncertainty of various theoretical expressions--for example, the energy levels of H and D required to obtain the Rydberg constant R_i from measurements of transition frequencies. We used an additive correction δ_i for each such expression, included those corrections among the variables of the least-squares adjustment, and took their estimated values as input data. The best a priori estimate of each δ_i was zero but with a standard uncertainty equal to the standard uncertainty of the theoretical expression.

Fourth, we analyzed the data using the method of least squares for correlated input data. Although the need to consider correlations among the input data in the evaluation of the fundamental constants was first emphasized well over half a century ago, the 1998 adjustment was the first time it was actually done.

As in the 1998 adjustment, the analysis of the input data proceeded in several stages. First, we compared the various measured values of each quantity. Next, by comparing values of a common inferred constant, principally α or h, we examined whether measured values of different quantities were consistent. Finally, we used the least-squares method as described above to carry out a multivariate analysis of the data. The focus of all those investigations was the compatibility of the data and the extent to which a particular datum would contribute to the 2002 recommended values of the constants.

The final least-squares adjustment used 105 of the 112 input data that were initially considered and 61 variables or adjusted constants whose values were determined by the least-squares algorithm. The input data included, for example, 27 H and D transition frequencies and frequency differences. Among the adjusted constants were R_i , α , h, and $A_r(e)$. Most of the recommended values in the 2002 CODATA set were calculated from the adjusted constants. For example, the elementary charge follows from the expression e $(2\alpha h/\mu_0 c)^{1/2}$, where $\mu_0 4\pi \times 10^{-7} \text{ N/A}^2$ is the magnetic constant and the speed of light c is defined to be 299 792 458 m/s. The uncertainties of

derived quantities are obtained from the uncertainties and covariances of the adjusted constants on which they depend.

A DISCREPANT MEASUREMENT

The primary difficulty with the input data uncovered in the course of the 2002 adjustment was a significant incompatibility of the value of $V_m(Si)$ with four measurements involving the Josephson constant K_J 2e/h and the von Klitzing constant R_K h/e²: two moving-coil watt-balance results for the product $K_J^2R_K$, a mercury-electrometer result for K_J , and a capacitor volt-balance result for K_J . The inconsistencies led us to consider whether relaxing either one or both of the assumptions that K_J 2e/h and R_K h/e² would reduce or possibly even eliminate the inconsistencies. Although both theory and experiment support the exactness of the assumed relations, we would have deemed our analysis incomplete had we not investigated possible modifications.

To that end, we assumed $K_{J}(2e/h)(1+\varepsilon_{J})$ and R_{K} $(h/e^2)(1+\epsilon_{_K})$, where $\epsilon_{_I}$ and $\epsilon_{_K}$ are unknown correction factors taken as additional adjusted constants. We set the initial input values of the correction factors to be zero, but gave them a sufficiently large uncertainty that their output values resulting from a least-squares adjustment were determined by other input data, not by those initial values. If we found that the adjusted values of the correction factors were statistically compatible with zero, then we could conclude that the experimental evidence suggested the relations K_{I} 2e/h and R_{K} h/e² were valid. On the other hand, an adjusted value of either of the correction factors that differed from zero in a statistically significant way would engender doubt about the exactness of the associated relation. We found no statistically significant deviations from zero for either ε_{r} or ε_{κ} .

The task group ultimately decided that, in the final least-squares adjustment, the a priori assigned uncertainties of the five incompatible input data would be weighted by a multiplicative factor 2.325. That weighting reduced the discrepancy between the value of $V_{\rm m}(Si)$ and the four other measurements to 1.5 standard deviations. As a consequence of the new $V_{\rm m}(Si)$ datum and the increased uncertainties, the 2002 recommended value of h is larger than the 1998 recommended value by a fractional amount of about

 8×10^{-8} , and its uncertainty is increased by about a factor of two, from $u_r = 7.8 \times 10^{-8}$ to $u_r = 1.7 \times 10^{-7}$. The 2002 CODATA set includes comparable changes in the recommended values and uncertainties of other constants, such as e, that depend strongly on h. Usually, new information leads to a reduction in uncertainties, but in this case new information has led to an increase.

REDUNDANCY IS SOLIDITY

Because there is little redundancy among some of the key input data, the 2002 CODATA set does not rest on as solid a foundation as one might wish. The constants α and h and the molar gas constant R play a critical role in determining many other constants, yet the recommended value of each is largely determined by a severely limited number of input data. Moreover, some of those data have rather different uncertainties u and hence rather different weights $1/u^2$.

The key input data used to determine α are the electron magnetic moment anomaly a_e and the quotient h/m(133 Cs). (The relative uncertainty of the quotient exceeds that of the anomaly by more than a factor of two.) Furthermore, only a single competitive experimental value of a_e exists, along with a single calculated value of the eighth-order coefficient $A_1^{(8)}$ in the theoretical expression for a_e based on quantum electrodynamics.

The two watt-balance values of $K_{\rm j}^2 R_{\rm k}$ are the key input data that determine h. The uncertainties in the two measurements differ by a factor of 2.3 and, as we have already discussed, the two measurements are incompatible with a measurement for the molar volume of Si.

For the molar gas constant, the key input data are based on two speed-of-sound measurements in argon: One of them used a spherical acoustic resonator; the other, an acoustic interferometer. The uncertainties of the two measurements differ by a factor of 4.7.

If our knowledge of the values of α , h, and R is to advance, we need additional input data that can provide for those constants uncertainties that are no larger than the current uncertainties. Ideally, the uncertainties would be considerably smaller than those of the current values.

New experimental and theoretical data that influence our knowledge of the values of the constants appear nearly continuously. And, thanks to the World Wide Web, it's easy to distribute new recommended values of the fundamental constants. Indeed, the 2002 CODATA set first appeared on the Web on 9 December 2003. The Web has also engendered new modes of work and thought--users expect that the information they find is up-to-date. For these reasons, the CODATA task group on fundamental constants decided at the time of the 1998 adjustment to take advantage of the high degree of computerization that had been incorporated in the 1998 compilation and to provide a new CODATA set of recommended values every 4 years: The 1213 years separating the first CODATA set⁴ of 1973, the second set³ of 1986, and the 1998 set² was no longer acceptable. The 2002 set is the first from the new schedule.

Based on the experience gained in preparing that set, we expect to maintain the new schedule in the future. The reader may therefore anticipate an updated fundamental constants article in the Physics Today Buyer's Guide in four years.

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Quantity	Symbol	Value	Unit	Relative standard
		TED CAX		uncertainty u _r
1 (1:1.:		ZERSAL	1	(,)
peed of light in vacuum	<i>c</i> , <i>c</i> ₀	299 792 458	m s ⁻¹	(exact)
nagnetic constant	$\mu_{\scriptscriptstyle 0}$	$4\pi \times 10^{-7}$	N A-2	()
1		$= 12.566\ 370\ 614\dots\times10^{-7}$	N A ⁻²	(exact)
lectric constant $1/\mu_0 c^2$	ϵ_0	8.854 187 817×10 ⁻¹²	F m ⁻¹	(exact)
haracteristic impedance of vacuum $\sqrt{\mu_0/\epsilon_0} = \mu_0 c$	Z_{0}	376.730 313 461	Ω	(exact)
lewtonian constant of gravitation	G	6.6742(10)×10 ⁻¹¹	m³ kg-1 s-2	1.5×10 ⁻⁴
	G/ħc	$6.7087(10)\times10^{-39}$	$(\text{GeV}/c^2)^{-2}$	1.5×10 ⁻⁴
anck constant	h	$6.626\ 0693(11)\times 10^{-34}$	J s	1.7×10 ⁻⁷
in eV s		$4.135\ 667\ 43(35)\times10^{-15}$	eV s	8.5×10 ⁻⁸
$h/2\pi$	\hbar	$1.054\ 571\ 68(18)\times 10^{-34}$	J s	1.7×10 ⁻⁷
in eV s		$6.582\ 119\ 15(56)\times 10^{-16}$	eV s	8.5×10^{-8}
ħc in MeV fm		197.326 968(17)	MeV fm	8.5×10^{-8}
lanck mass (ħc/G) ^{1/2}	$m_{ m P}$	2.176 45(16)×10 ⁻⁸	kg	7.5×10 ⁻⁵
lanck temperature $(\hbar c^5/G)^{1/2}/k$	$T_{ m P}$	$1.41679(11) \times 10^{32}$	K	7.5×10^{-5}
lanck length $\hbar/m_{\rm p}c = (\hbar G/c^3)^{1/2}$	$l_{ m P}$	$1.616\ 24(12)\times10^{-35}$	m	7.5×10^{-5}
lanck time $l_P/c = (\hbar G/c^5)^{1/2}$	$\dot{t_{ m P}}$	5.391 21(40)×10 ⁻⁴⁴	S	7.5×10 ⁻⁵
	ELECTRO	DMAGNETIĆ		
ementary charge	е	1.602 176 53(14)×10 ⁻¹⁹	С	8.5×10 ⁻⁸
	e/h	2.417 989 40(21)×10 ¹⁴	$A J^{-1}$	8.5×10 ⁻⁸
agnetic flux quantum h/2e	$\Phi_{\scriptscriptstyle 0}$	$2.067\ 833\ 72(18)\times10^{-15}$	Wb	8.5×10 ⁻⁸
onductance quantum 2e²/h	G_{0}	$7.748\ 091\ 733(26) \times 10^{-5}$	S	3.3×10 ⁻⁹
inverse of conductance quantum	G_0^{-1}	12 906.403 725(43)	Ω	3.3×10 ⁻⁹
osephson constant ^a 2e/h	K_{I}	483 597.879(41)×10°	Hz V ⁻¹	8.5×10^{-8}
on Klitzing constant ^b $h/e^2 = \mu_0 c/2\alpha$	$R_{ m K}^{^{ m J}}$	25 812.807 449(86)	Ω	3.3×10 ⁻⁹
ohr magneton eħ/2m _e	$\mu_{ ext{B}}^{ ext{R}}$	927.400 949(80)×10 ⁻²⁶	J T ⁻¹	8.6×10 ⁻⁸
in eV T ⁻¹	1 Б	$5.788\ 381\ 804(39)\times10^{-5}$	eV T-1	6.7×10 ⁻⁹
	$\mu_{\scriptscriptstyle m B}/h$	13.996 2458(12)×10 ⁹	Hz T ⁻¹	8.6×10 ⁻⁸
	$\mu_{\rm B}/hc$	46.686 4507(40)	m ⁻¹ T ⁻¹	8.6×10 ⁻⁸
	$\mu_{\rm B}/k$	0.671 7131(12)	K T ⁻¹	1.8×10 ⁻⁶
uclear magneton eħ/2mp		$5.05078343(43)\times10^{-27}$	J T-1	8.6×10 ⁻⁸
in eV T ⁻¹	$\mu_{ m N}$		eV T ⁻¹	6.7×10 ⁻⁹
iii ev 1	/1-	3.152 451 259(21)×10 ⁻⁸		
	$\mu_{\rm N}/h$	7.622 593 71(65)	MHz T ⁻¹	8.6×10 ⁻⁸
	$\mu_{\rm N}/hc$	2.542 623 58(22)×10 ⁻²	m ⁻¹ T ⁻¹	8.6×10 ⁻⁸
	$\mu_{\rm N}/k$	3.658 2637(64)×10 ⁻⁴ AND NUCLEAR	K T ⁻¹	1.8×10 ⁻⁶
		General		
ne-structure constant $e^2/4\pi\epsilon_0\hbar c$	α	$7.297\ 352\ 568(24)\times10^{-3}$		3.3×10 ⁻⁹
inverse fine-structure constant	α^{-1}	137.035 999 11(46)		3.3×10 ⁻⁹
ydberg constant $\alpha^2 m_e c/2h$	R_{∞}	10 973 731.568 525(73)	m ⁻¹	6.6×10 ⁻¹²
y aberg constant a met 217	$R_{\infty}^{\infty}c$	$3.289 841 960 360(22) \times 10^{15}$	Hz	6.6×10 ⁻¹²
		$2.179\ 872\ 09(37)\times10^{-18}$	J	1.7×10 ⁻⁷
P. hair aV	$R_{\infty}hc$.` .'	eV	8.5×10 ⁻⁸
$R_{\infty}hc$ in eV		13.605 6923(12)		
ohr radius $\alpha/4\pi R_{\infty} = 4\pi\epsilon_0 \hbar^2/m_e e^2$	<i>a</i> ₀	$0.529\ 177\ 2108(18) \times 10^{-10}$	m T	3.3×10 ⁻⁹
Hartree energy $e^2/4\pi\epsilon_0 a_0 = 2R_\infty hc = \alpha^2 m_e c^2$	$E_{ m h}$	4.359 744 17(75)×10 ⁻¹⁸	J	1.7×10 ⁻⁷
in eV		27.211 3845(23)	eV	8.5×10 ⁻⁸
			$m^2 s^{-1}$	6.7×10 ⁻⁹
	$h/2m_e$	3.636 947 550(24)×10 ⁻⁴		
	h/m_e^{c}	7.273 895 101(48)×10 ⁻⁴	$m^2 s^{-1}$	6.7×10 ⁻⁹
uantum of circulation	h/m_e Ele	7.273 895 101(48)×10 ⁻⁴ ctroweak	m ² s ⁻¹	
uantum of circulation ermi coupling constant ^c	h/m_e^{c}	7.273 895 101(48)×10 ⁻⁴		6.7×10 ⁻⁹ 8.6×10 ⁻⁶
uantum of circulation ermi coupling constant c reak mixing angle d $ heta_{ m W}$ (on-shell scheme)	h/m_e Elec $G_F/(\hbar c)^3$	7.273 895 101(48)×10 ⁻⁴ ctroweak 1.166 39(1)×10 ⁻⁵	m ² s ⁻¹	8.6×10 ⁻⁶
nantum of circulation	h/m_e Elec $G_F/(\hbar c)^3$ $\sin^2 \theta_W$	7.273 895 101(48)×10 ⁻⁴ etroweak 1.166 39(1)×10 ⁻⁵ 0.222 15(76)	m ² s ⁻¹	
ermi coupling constant ^c eak mixing angle ^d $\theta_{\rm W}$ (on-shell scheme) $\sin^2 \theta_{\rm W} = s_{\rm W}^2 \equiv 1 - (m_{\rm W}/m_{\rm Z})^2$	h/m_e Ele $G_F/(\hbar c)^3$ $\sin^2 \theta_W$ Ele	7.273 895 101(48)×10 ⁻⁴ ctroweak 1.166 39(1)×10 ⁻⁵ 0.222 15(76) ectron, e ⁻	$m^2 s^{-1}$ GeV^{-2}	8.6×10 ⁻⁶ 3.4×10 ⁻³
ermi coupling constant ^c eak mixing angle ^d $\theta_{\rm W}$ (on-shell scheme) $\sin^2 \theta_{\rm W} = s_{\rm W}^2 \equiv 1 - (m_{\rm W}/m_{\rm Z})^2$ ectron mass	$h/m_{\rm e}$ Elec $G_{\rm F}/(\hbar c)^3$ $\sin^2 \theta_{\rm W}$ Elec $m_{\rm e}$	7.273 895 101(48)×10 ⁻⁴ ctroweak 1.166 39(1)×10 ⁻⁵ 0.222 15(76) cetron, e ⁻ 9.109 3826(16)×10 ⁻³¹	m² s-1 GeV-2 kg	8.6×10 ⁻⁶ 3.4×10 ⁻³ 1.7×10 ⁻⁷
ermi coupling constant ^c eak mixing angle ^d $\theta_{\rm W}$ (on-shell scheme) $\sin^2 \theta_{\rm W} = s_{\rm W}^2 \equiv 1 - (m_{\rm W}/m_{\rm Z})^2$ ectron mass in u, $m_{\rm c} = A_{\rm r}({\rm e})$ u (electron rel. atomic mass times u)	h/m_e Ele $G_F/(\hbar c)^3$ $\sin^2 \theta_W$ Ele m_e	7.273 895 101(48)×10 ⁻⁴ ctroweak 1.166 39(1)×10 ⁻⁵ 0.222 15(76) cctron, e ⁻ 9.109 3826(16)×10 ⁻³¹ 5.485 799 0945(24)×10 ⁻⁴	m ² s ⁻¹ GeV ⁻² kg u	8.6×10 ⁻⁶ 3.4×10 ⁻³ 1.7×10 ⁻⁷ 4.4×10 ⁻¹⁰
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ermi coupling constant ^c eak mixing angle ^d $\theta_{\rm W}$ (on-shell scheme) $\sin^2 \theta_{\rm W} = s_{\rm W}^2 \equiv 1 - (m_{\rm W}/m_{\rm Z})^2$ ectron mass in u, $m_{\rm e} = A_{\rm r}({\rm e})$ u (electron rel. atomic mass times u) energy equivalent in MeV ectron–muon mass ratio	h/m_e Elec $G_F/(\hbar c)^3$ $\sin^2 \theta_W$ Elec m_e	7.273 895 101(48)×10 ⁻⁴ ctroweak 1.166 39(1)×10 ⁻⁵ 0.222 15(76) cetron, e ⁻ 9.109 3826(16)×10 ⁻³¹ 5.485 799 0945(24)×10 ⁻⁴ 8.187 1047(14)×10 ⁻¹⁴ 0.510 998 918(44)	m ² s ⁻¹ GeV ⁻² kg u J	8.6×10 ⁻⁶ 3.4×10 ⁻³ 1.7×10 ⁻⁷ 4.4×10 ⁻¹⁰ 1.7×10 ⁻⁷ 8.6×10 ⁻⁸
ermi coupling constant ^c reak mixing angle ^d $\theta_{\rm W}$ (on-shell scheme) $\sin^2 \theta_{\rm W} = s_{\rm W}^2 \equiv 1 - (m_{\rm W}/m_{\rm Z})^2$ ectron mass in u, $m_{\rm e} = A_{\rm r}({\rm e})$ u (electron rel. atomic mass times u) energy equivalent in MeV ectron-muon mass ratio ectron-tau mass ratio	h/m_e Elec $G_F/(\hbar c)^3$ $\sin^2 \theta_W$ Elec m_e $m_e c^2$ m_e/m_μ	7.273 895 101(48)×10 ⁻⁴ ctroweak 1.166 39(1)×10 ⁻⁵ 0.222 15(76) ectron, e ⁻ 9.109 3826(16)×10 ⁻³¹ 5.485 799 0945(24)×10 ⁻⁴ 8.187 1047(14)×10 ⁻¹⁴ 0.510 998 918(44) 4.836 331 67(13)×10 ⁻³	m ² s ⁻¹ GeV ⁻² kg u J	8.6×10 ⁻⁶ 3.4×10 ⁻³ 1.7×10 ⁻⁷ 4.4×10 ⁻¹⁰ 1.7×10 ⁻⁷ 8.6×10 ⁻⁸ 2.6×10 ⁻⁸
ermi coupling constant ^c eak mixing angle ^d $\theta_{\rm W}$ (on-shell scheme) $\sin^2 \theta_{\rm W} = s_{\rm W}^2 \equiv 1 - (m_{\rm W}/m_{\rm Z})^2$ ectron mass in u, $m_{\rm e} = A_{\rm r}({\rm e})$ u (electron rel. atomic mass times u) energy equivalent in MeV ectron–muon mass ratio ectron–tau mass ratio ectron–proton mass ratio	h/m_e Elec $G_{\rm F}/(\hbar c)^3$ $\sin^2 \theta_{\rm W}$ Elec m_e m_e m_e/m_μ m_e/m_τ m_e/m_p	7.273 895 101(48)×10 ⁻⁴ ctroweak 1.166 39(1)×10 ⁻⁵ 0.222 15(76) ectron, e ⁻ 9.109 3826(16)×10 ⁻³¹ 5.485 799 0945(24)×10 ⁻⁴ 8.187 1047(14)×10 ⁻¹⁴ 0.510 998 918(44) 4.836 331 67(13)×10 ⁻³ 2.875 64(47)×10 ⁻⁴ 5.446 170 2173(25)×10 ⁻⁴	m ² s ⁻¹ GeV ⁻² kg u J	8.6×10 ⁻⁶ 3.4×10 ⁻³ 1.7×10 ⁻⁷ 4.4×10 ⁻¹⁰ 1.7×10 ⁻⁷ 8.6×10 ⁻⁸ 2.6×10 ⁻⁸ 1.6×10 ⁻⁴
ermi coupling constant ^c eak mixing angle ^d $\theta_{\rm W}$ (on-shell scheme) $\sin^2 \theta_{\rm W} = s_{\rm W}^2 \equiv 1 - (m_{\rm W}/m_{\rm Z})^2$ ectron mass in u, $m_{\rm e} = A_{\rm r}({\rm e})$ u (electron rel. atomic mass times u) energy equivalent in MeV ectron-muon mass ratio ectron-tau mass ratio ectron-proton mass ratio ectron-neutron mass ratio	h/m_e Elec $G_{\rm F}/(\hbar c)^3$ $\sin^2 \theta_{\rm W}$ Elec m_e $m_e c^2$ m_e/m_μ m_e/m_τ m_e/m_p m_e/m_n	7.273 895 101(48)×10 ⁻⁴ ctroweak 1.166 39(1)×10 ⁻⁵ 0.222 15(76) ctron, e ⁻ 9.109 3826(16)×10 ⁻³¹ 5.485 799 0945(24)×10 ⁻⁴ 8.187 1047(14)×10 ⁻¹⁴ 0.510 998 918(44) 4.836 331 67(13)×10 ⁻³ 2.875 64(47)×10 ⁻⁴ 5.446 170 2173(25)×10 ⁻⁴ 5.438 673 4481(38)×10 ⁻⁴	m ² s ⁻¹ GeV ⁻² kg u J	8.6×10 ⁻⁶ 3.4×10 ⁻³ 1.7×10 ⁻⁷ 4.4×10 ⁻¹⁰ 1.7×10 ⁻⁷ 8.6×10 ⁻⁸ 2.6×10 ⁻⁸ 1.6×10 ⁻⁴ 4.6×10 ⁻¹⁰ 7.0×10 ⁻¹⁰
ermi coupling constant ^c reak mixing angle ^d $\theta_{\rm W}$ (on-shell scheme) $\sin^2 \theta_{\rm W} = s_{\rm W}^2 \equiv 1 - (m_{\rm W}/m_{\rm Z})^2$ electron mass in u, $m_{\rm e} = A_{\rm r}({\rm e})$ u (electron rel. atomic mass times u) energy equivalent in MeV lectron-muon mass ratio lectron-tau mass ratio lectron-proton mass ratio lectron-neutron mass ratio lectron-deuteron mass ratio	h/m_e Ele $G_{\rm F}/(\hbar c)^3$ $\sin^2 \theta_{\rm W}$ Ele m_e $m_e c^2$ m_e/m_μ m_e/m_τ $m_e/m_{\rm P}$ $m_e/m_{\rm m}$ $m_e/m_{\rm m}$	7.273 895 101(48)×10 ⁻⁴ ctroweak 1.166 39(1)×10 ⁻⁵ 0.222 15(76) ctron, e ⁻ 9.109 3826(16)×10 ⁻³¹ 5.485 799 0945(24)×10 ⁻⁴ 8.187 1047(14)×10 ⁻¹⁴ 0.510 998 918(44) 4.836 331 67(13)×10 ⁻³ 2.875 64(47)×10 ⁻⁴ 5.446 170 2173(25)×10 ⁻⁴ 5.438 673 4481(38)×10 ⁻⁴ 2.724 437 1095(13)×10 ⁻⁴	m ² s ⁻¹ GeV ⁻² kg u J	8.6×10 ⁻⁶ 3.4×10 ⁻³ 1.7×10 ⁻⁷ 4.4×10 ⁻¹⁰ 1.7×10 ⁻⁷ 8.6×10 ⁻⁸ 2.6×10 ⁻⁸ 1.6×10 ⁻⁴ 4.6×10 ⁻¹⁰ 7.0×10 ⁻¹⁰ 4.8×10 ⁻¹⁰
ermi coupling constant ereak mixing angle $^d\theta_{\rm W}$ (on-shell scheme) $\sin^2\theta_{\rm W}=s_{\rm W}^2\equiv 1-(m_{\rm W}/m_{\rm Z})^2$ electron mass in u, $m_{\rm e}=A_{\rm r}({\rm e})$ u (electron rel. atomic mass times u) energy equivalent in MeV electron-muon mass ratio electron-proton mass ratio electron-neutron mass ratio electron-neutron mass ratio electron-neutron mass ratio	h/m_e Elec $G_{\rm F}/(\hbar c)^3$ $\sin^2 \theta_{\rm W}$ Elec m_e $m_e c^2$ m_e/m_μ m_e/m_τ m_e/m_p m_e/m_n	7.273 895 101(48)×10 ⁻⁴ ctroweak 1.166 39(1)×10 ⁻⁵ 0.222 15(76) ctron, e ⁻ 9.109 3826(16)×10 ⁻³¹ 5.485 799 0945(24)×10 ⁻⁴ 8.187 1047(14)×10 ⁻¹⁴ 0.510 998 918(44) 4.836 331 67(13)×10 ⁻³ 2.875 64(47)×10 ⁻⁴ 5.446 170 2173(25)×10 ⁻⁴ 5.438 673 4481(38)×10 ⁻⁴	m ² s ⁻¹ GeV ⁻² kg u J	8.6×10 ⁻⁶ 3.4×10 ⁻³ 1.7×10 ⁻⁷ 4.4×10 ⁻¹⁰ 1.7×10 ⁻⁷ 8.6×10 ⁻⁸ 2.6×10 ⁻⁸ 1.6×10 ⁻⁴ 4.6×10 ⁻¹⁰ 7.0×10 ⁻¹⁰

CODATA Recommended Values of	the Fun	damental Physical (Zonstants –	- 2002
Quantity	Symbol	Value	Unit	Relative standard uncertainty u_r
Compton wavelength $h/m_{\rm e}c$	$\lambda_{\rm C}$	2.426 310 238(16)×10 ⁻¹²	m	6.7×10 ⁻⁹
$\lambda_C/2\pi = \alpha a_0 = \alpha^2/4\pi R_\infty$	χ̈́ _C	$386.159\ 2678(26) \times 10^{-15}$	m	6.7×10 ⁻⁹
lassical electron radius $\alpha^2 a_0$	$r_{\rm e}$	$2.817\ 940\ 325(28)\times 10^{-15}$	m	1.0×10 ⁻⁸
homson cross section $(8\pi/3)r_e^2$	σ_{e}	$0.665\ 245\ 873(13)\times10^{-28}$	m^2	2.0×10 ⁻⁸
ectron magnetic moment	$\mu_{ m e}$	$-928.476\ 412(80)\times10^{-26}$	J T-1	8.6×10 ⁻⁸
to Bohr magneton ratio	$\mu_{ m e}^{\prime}/\mu_{ m B}$	-1.001 159 652 1859(38)	J -	3.8×10 ⁻¹²
to nuclear magneton ratio	$\mu_{\rm e}/\mu_{ m N}$	-1838.281 971 07(85)		4.6×10 ⁻¹⁰
		$1.159\ 652\ 1859(38) \times 10^{-3}$		3.2×10 ⁻⁹
ectron magnetic moment anomaly $ \mu_e /\mu_B-1$	$a_{\rm e}$	* * *		
lectron g-factor $-2(1+a_e)$	g _e	-2.002 319 304 3718(75)		3.8×10 ⁻¹²
ectron-muon magnetic moment ratio	$\mu_{ m e}/\mu_{\mu}$	206.766 9894(54)		2.6×10 ⁻⁸
ectron-proton magnetic moment ratio ectron to shielded proton magnetic moment ratio	$\mu_{ m e}/\mu_{ m p}$	-658.210 6862(66)		1.0×10 ⁻⁸
(H ₂ O, sphere, 25 °C)	$\mu_{_{ m e}}/\mu_{_{ m p}}'$	-658.227 5956(71)		1.1×10 ⁻⁸
lectron-neutron magnetic moment ratio	$\mu_{ m e}/\mu_{ m n}$	960.920 50(23)		2.4×10^{-7}
lectron-deuteron magnetic moment ratio	$\mu_{\rm e}/\mu_{ m d}$	-2143.923 493(23)		1.1×10^{-8}
lectron to shielded helion ^e magnetic moment ratio				
(gas, sphere, 25 °C)	$\mu_{ m e}/\mu_{ m h}'$	864.058 255(10)		1.2×10 ⁻⁸
electron gyromagnetic ratio $2 \mu_e /\hbar$	$\gamma_{\rm e}$	$1.760\ 859\ 74(15)\times10^{11}$	$s^{-1} T^{-1}$	8.6×10 ⁻⁸
5/	$\gamma_{ m e} / 2\pi$	28 024.9532(24)	MHz T ⁻¹	8.6×10 ⁻⁸
	Muon		1,1111	3.0/(10
nuon mass	m_{μ}	1.883 531 40(33)×10 ⁻²⁸	kg	1.7×10 ⁻⁷
in u, $m_{\mu} = A_{\rm r}(\mu)$ u (muon rel. atomic mass times u)	μ	0.113 428 9264(30)	u	2.6×10 ⁻⁸
energy equivalent	$m_{\mu}c^2$	$1.69283360(29)\times10^{-11}$	J	1.7×10 ⁻⁷
in MeV	m_{μ} c	105.658 3692(94)	J MeV	8.9×10 ⁻⁸
	,		Ivie v	
nuon-electron mass ratio	$m_{\mu}/m_{\rm e}$	206.768 2838(54)		2.6×10 ⁻⁸
nuon–tau mass ratio	$m_{\mu}/m_{ au}$	$5.945\ 92(97)\times10^{-2}$		1.6×10 ⁻⁴
nuon–proton mass ratio	$m_{\mu}/m_{ m p}$	0.112 609 5269(29)		2.6×10 ⁻⁸
nuon-neutron mass ratio	$m_{\mu}/m_{\rm n}$	0.112 454 5175(29)		2.6×10 ⁻⁸
muon molar mass $N_{ m A} m_{\mu}$	$M(\mu), M_{\mu}$	$0.113\ 428\ 9264(30)\times10^{-3}$	kg mol ⁻¹	2.6×10 ⁻⁸
nuon Compton wavelength $h/m_{\mu}c$	$\lambda_{\mathrm{C},\mu}$	$11.734\ 441\ 05(30)\times 10^{-15}$	m	2.5×10^{-8}
$\lambda_{C,\mu}/2\pi$	$\chi_{C,\mu}$	1.867 594 298(47)×10 ⁻¹⁵	m	2.5×10 ⁻⁸
nuon magnetic moment	μ_{μ}	$-4.490\ 447\ 99(40)\times10^{-26}$	J T ⁻¹	8.9×10 ⁻⁸
to Bohr magneton ratio	$\mu_{\mu}^{\mu}/\mu_{ m B}$	$-4.841\ 970\ 45(13)\times10^{-3}$	3	2.6×10 ⁻⁸
to nuclear magneton ratio	$\mu_{\mu}/\mu_{ m N}$	-8.890 596 98(23)		2.6×10 ⁻⁸
muon magnetic moment anomaly $ \mu_{\mu} /(e\hbar/2m_{\mu})$ –1		$1.165\ 919\ 81(62)\times10^{-3}$		5.3×10 ⁻⁷
	a_{μ}			
nuon g-factor $-2(1+a_{\mu})$	8 _μ	-2.002 331 8396(12)		6.2×10 ⁻¹⁰
nuon-proton magnetic moment ratio	μ _μ /μ _p Tau	-3.183 345 118(89)		2.8×10 ⁻⁸
au mass ^f	m_{τ}	3.167 77(52)×10 ⁻²⁷	kg	1.6×10 ⁻⁴
in u, $m_{\tau} = A_r(\tau)$ u (tau rel. atomic mass times u)	··· τ	1.907 68(31)	u	1.6×10 ⁻⁴
	2	1 1 4		
energy equivalent	$m_{\tau}c^2$	2.847 05(46)×10 ⁻¹⁰	J	1.6×10 ⁻⁴
in MeV	,	1776.99(29)	MeV	1.6×10 ⁻⁴
au–electron mass ratio	$m_{\tau}/m_{\rm e}$	3477.48(57)		1.6×10 ⁻⁴
au-muon mass ratio	$m_{ au}/m_{\mu}$	16.8183(27)		1.6×10 ⁻⁴
au–proton mass ratio	$m_{ au}/m_{ m p}$	1.893 90(31)		1.6×10 ⁻⁴
au–neutron mass ratio	$m_{ au}/m_{ m n}$	1.891 29(31)		1.6×10 ⁻⁴
au molar mass $N_{ m A} m_{ au}$	$M(\tau)$, M_{τ}	$1.907 68(31) \times 10^{-3}$	kg mol ⁻¹	1.6×10 ⁻⁴
au Compton wavelength $h/m_{\tau}c$	$\lambda_{\mathrm{C}, au}$	$0.69772(11)\times10^{-15}$	m	1.6×10 ⁻⁴
$\lambda_{\mathrm{C}, au}/2\pi$	$\chi_{C,\tau}$	$0.111\ 046(18)\times10^{-15}$	m	1.6×10 ⁻⁴
		oton, p		
roton mass	$m_{ m p}$	$1.672\ 621\ 71(29)\times 10^{-27}$	kg	1.7×10 ⁻⁷
in u, $m_p = A_r(p)$ u (proton rel. atomic mass times u)		1.007 276 466 88(13)	u	1.3×10 ⁻¹⁰
energy equivalent	$m_{\rm p} c^2$	1.503 277 43(26)×10 ⁻¹⁰	J	1.7×10 ⁻⁷
in MeV		938.272 029(80)	MeV	8.6×10 ⁻⁸
proton-electron mass ratio	$m_{\rm p}/m_{\rm e}$	1836.152 672 61(85)		4.6×10 ⁻¹⁰
proton–muon mass ratio	$m_{\rm p}/m_{\mu}$	8.880 243 33(23)		2.6×10 ⁻⁸
oroton-tau mass ratio	$m_{ m p}/m_{ m p}$	0.528 012(86)		1.6×10 ⁻⁴
proton–neutron mass ratio				5.8×10 ⁻¹⁰
	$m_{\rm p}/m_{\rm n}$	0.998 623 478 72(58)	Clra-1	
proton charge to mass quotient	$e/m_{\rm p}$	9.578 833 76(82)×10 ⁷	C kg ⁻¹	8.6×10 ⁻⁸
proton molar mass $N_{\rm A} m_{\rm p}$	$M(p), M_p$	1.007 276 466 88(13)×10 ⁻³	kg mol ⁻¹	1.3×10 ⁻¹⁰
	1	$1.321\ 409\ 8555(88)\times 10^{-15}$	m	6.7×10 ⁻⁹
proton Compton wavelength $h/m_{ m p}c$ $\lambda_{ m C,p}/2\pi$	$\lambda_{C,p}$ $\chi_{C,p}$	$0.210\ 308\ 9104(14)\times10^{-15}$	111	6.7×10 ⁻⁹

Quantity	Symbol	Value	Unit	Relative standard
				uncertainty u _r
roton rms charge radius	$R_{\rm p}$	$0.8750(68) \times 10^{-15}$	m	7.8×10^{-3}
roton magnetic moment	$\mu_{ extsf{p}}$	$1.410\ 606\ 71(12)\times10^{-26}$	J T ⁻¹	8.7×10 ⁻⁸
to Bohr magneton ratio	$\mu_{ m p}/\mu_{ m B}$	$1.521\ 032\ 206(15)\times 10^{-3}$		1.0×10 ⁻⁸
to nuclear magneton ratio	$\mu_{ m p}/\mu_{ m N}$	2.792 847 351(28)		1.0×10 ⁻⁸
roton g-factor $2\mu_{ m p}/\mu_{ m N}$	g _p	5.585 694 701(56)		1.0×10 ⁻⁸
roton-neutron magnetic moment ratio	$\mu_{\scriptscriptstyle \mathrm{p}}/\mu_{\scriptscriptstyle \mathrm{n}}$	-1.459 898 05(34)		2.4×10^{-7}
hielded proton magnetic moment				
(H ₂ O, sphere, 25 °C)	$\mu_{\mathtt{p}}'$	$1.410\ 570\ 47(12)\times 10^{-26}$	J T ⁻¹	8.7×10^{-8}
to Bohr magneton ratio	$\mu_{ m p}'/\mu_{ m B}$	$1.520\ 993\ 132(16)\times 10^{-3}$		1.1×10^{-8}
to nuclear magneton ratio	$\mu_{ m p}'/\mu_{ m N}$	2.792 775 604(30)		1.1×10^{-8}
roton magnetic shielding correction 1 – $\mu_{\rm p}'/\mu_{\rm p}$	•			
(H ₂ O, sphere, 25 °C)	$\sigma_{\scriptscriptstyle m p}'$	25.689(15)×10 ⁻⁶		5.7×10 ⁻⁴
roton gyromagnetic ratio $2\mu_{ m p}/\hbar$	$\gamma_{\rm p}^{\rm r}$	2.675 222 05(23)×10 ⁸	$s^{-1} T^{-1}$	8.6×10^{-8}
<i>o, o</i> , , ,	$\gamma_{\rm p}/2\pi$	42.577 4813(37)	$ m MHz~T^{-1}$	8.6×10^{-8}
nielded proton gyromagnetic ratio $2\mu_{_{ m p}}^{\prime}/\hbar$, b	()		
(H ₂ O, sphere, 25 °C)	$\gamma_{\rm p}'$	2.675 153 33(23)×10 ⁸	$s^{-1} T^{-1}$	8.6×10 ⁻⁸
(2-,,)	$\gamma_{\rm p}^{\rm p}/2\pi$	42.576 3875(37)	MHz T ⁻¹	8.6×10 ⁻⁸
		eutron, n		2.3/1.20
eutron mass	$m_{\rm n}$	1.674 927 28(29)×10 ⁻²⁷	kg	1.7×10 ⁻⁷
in u, $m_n = A_r(n)$ u (neutron rel. atomic mass times u		1.008 664 915 60(55)	u	5.5×10 ⁻¹⁰
energy equivalent	$m_{\rm n}c^2$	$1.505\ 349\ 57(26)\times10^{-10}$	J	1.7×10 ⁻⁷
in MeV	m _n c	939.565 360(81)	J MeV	
	m /	` ' .	INTE A	8.6×10 ⁻⁸ 7.0×10 ⁻¹⁰
eutron-electron mass ratio	$m_{\rm n}/m_{\rm e}$	1838.683 6598(13)		
eutron-muon mass ratio	$m_{\rm n}/m_{\mu}$	8.892 484 02(23)		2.6×10 ⁻⁸
eutron-tau mass ratio	$m_{_{ m II}}/m_{_{ m T}}$	0.528 740(86)		1.6×10 ⁻⁴
eutron-proton mass ratio	$m_{\rm n}/m_{\rm p}$	1.001 378 418 70(58)		5.8×10 ⁻¹⁰
eutron molar mass $N_{\rm A}m_{\rm n}$	$M(n), M_n$	$1.008\ 664\ 915\ 60(55)\times 10^{-3}$	kg mol ⁻¹	5.5×10 ⁻¹⁰
eutron Compton wavelength $h/m_n c$	$\lambda_{\mathrm{C,n}}$	$1.319\ 590\ 9067(88) \times 10^{-15}$	m	6.7×10 ⁻⁹
$\lambda_{\mathrm{C,n}}/2\pi$	$\chi_{C,n}$	$0.210\ 019\ 4157(14)\times10^{-15}$	m	6.7×10 ⁻⁹
eutron magnetic moment	$\mu_{\scriptscriptstyle m n}$	$-0.966\ 236\ 45(24)\times10^{-26}$	J T ⁻¹	2.5×10 ⁻⁷
to Bohr magneton ratio	$\mu_{\scriptscriptstyle m n}/\mu_{\scriptscriptstyle m B}$	$-1.041\ 875\ 63(25)\times10^{-3}$		2.4×10 ⁻⁷
to nuclear magneton ratio	$\mu_{ m n}/\mu_{ m N}$	-1.913 042 73(45)		2.4×10 ⁻⁷
eutron g-factor $2\mu_{ m n}/\mu_{ m N}$	g_n	-3.826 085 46(90)		2.4×10 ⁻⁷
eutron-electron magnetic moment ratio	$\mu_{ m n}/\mu_{ m e}$	$1.040\ 668\ 82(25)\times10^{-3}$		2.4×10 ⁻⁷
eutron-proton magnetic moment ratio	$\mu_{\scriptscriptstyle m n}/\mu_{\scriptscriptstyle m p}$	-0.684 979 34(16)		2.4×10 ⁻⁷
eutron to shielded proton magnetic moment ratio	. н. р	. ,		
(H ₂ O, sphere, 25 °C)	$\mu_{ m n}/\mu_{ m p}'$	-0.684 996 94(16)		2.4×10 ⁻⁷
eutron gyromagnetic ratio $2 \mu_n /\hbar$	γ_n	1.832 471 83(46)×10 ⁸	$s^{-1} T^{-1}$	2.5×10 ⁻⁷
(/ n	$\gamma_{\rm n}^{\rm n}/2\pi$	29.164 6950(73)	MHz T ⁻¹	2.5×10 ⁻⁷
	De	uteron, d	111111111111111111111111111111111111111	2107.120
euteron mass		3.343 583 35(57)×10 ⁻²⁷	kg	1.7×10 ⁻⁷
in u, $m_d = A_r(d)$ u (deuteron rel. atomic mass times u	$m_{\rm d}$	2.013 553 212 70(35)	_	1.7×10 ⁻¹⁰
			u T	1.7×10 ⁻⁷
energy equivalent	$m_{\rm d}c^2$	$3.005\ 062\ 85(51)\times10^{-10}$	J MoV	
ın MeV	/.	1875.612 82(16)	MeV	8.6×10 ⁻⁸
euteron–electron mass ratio	$m_{\rm d}/m_{\rm e}$	3670.482 9652(18)		4.8×10 ⁻¹⁰
euteron–proton mass ratio	$m_{\rm d}/m_{\rm p}$	1.999 007 500 82(41)	1 1-1	2.0×10 ⁻¹⁰
euteron molar mass $N_{\rm A}m_{\rm d}$	$M(d), M_d$	$2.013\ 553\ 212\ 70(35) \times 10^{-3}$	kg mol ⁻¹	1.7×10 ⁻¹⁰
euteron rms charge radius	$R_{\rm d}$	2.1394(28)×10 ⁻¹⁵	m	1.3×10 ⁻³
euteron magnetic moment	$\mu_{ m d}$	$0.433\ 073\ 482(38) \times 10^{-26}$	J T ⁻¹	8.7×10 ⁻⁸
to Bohr magneton ratio	$\mu_{ m d}/\mu_{ m B}$	$0.466\ 975\ 4567(50)\times10^{-3}$		1.1×10 ⁻⁸
to nuclear magneton ratio	$\mu_{ m d}/\mu_{ m N}$	0.857 438 2329(92)		1.1×10 ⁻⁸
euteron-electron magnetic moment ratio	$\mu_{ m d}/\mu_{ m e}$	$-4.664\ 345\ 548(50)\times10^{-4}$		1.1×10 ⁻⁸
euteron-proton magnetic moment ratio	$\mu_{ m d}/\mu_{ m p}$	0.307 012 2084(45)		1.5×10 ⁻⁸
euteron–neutron magnetic moment ratio	$\mu_{ m d}/\mu_{ m n}$	-0.448 206 52(11)		2.4×10 ⁻⁷
		Helion, h		
elion mass ^e	$m_{ m h}$	5.006 412 14(86)×10 ⁻²⁷	kg	1.7×10 ⁻⁷
in u, $m_h = A_r(h)$ u (helion rel. atomic mass times u)	п	3.014 932 2434(58)	u	1.9×10 ⁻⁹
energy equivalent	$m_{ m h}c^2$	4.499 538 84(77)×10 ⁻¹⁰	J	1.7×10 ⁻⁷
in MeV	·· n-	2808.391 42(24)	MeV	8.6×10 ⁻⁸
elion–electron mass ratio	$m_{\rm h}/m_{\rm e}$	5495.885 269(11)	1,10 /	2.0×10 ⁻⁹
elion–proton mass ratio		2.993 152 6671(58)		1.9×10 ⁻⁹
	$m_{\rm h}/m_{\rm p}$	1 1	kg mol ⁻¹	1.9×10 ⁻⁹
nelion molar mass N _A m _h hielded helion magnetic moment (gas, sphere, 25 °C)	$M(h), M_h$	$3.014\ 932\ 2434(58) \times 10^{-3}$	I T -1	8.7×10 ⁻⁸
	$\mu_{\mathrm{h}}^{\prime}$	$-1.074\ 553\ 024(93)\times10^{-26}$	J I	0./ 10
to Bohr magneton ratio	$\mu'_{ m h}/\mu_{ m B}$	$-1.158\ 671\ 474(14)\times10^{-3}$	_	1.2×10 ⁻⁸

Quantity	Symbol	Value	Unit	Relative standard uncertainty u_r
to nuclear magneton ratio hielded helion to proton magnetic moment ratio	$\mu_{\mathrm{h}}^\prime/\mu_{\mathrm{N}}$	-2.127 497 723(25)		1.2×10 ⁻⁸
(gas, sphere, 25 °C) hielded helion to shielded proton magnetic moment	$\mu_{\mathrm{h}}^\prime/\mu_{\mathrm{p}}$	-0.761 766 562(12)		1.5×10 ⁻⁸
ratio (gas/H ₂ O, spheres, 25 °C)	$\mu_{ ext{h}}^{\prime}/\mu_{ ext{p}}^{\prime}$	-0.761 786 1313(33)		4.3×10 ⁻⁹
shielded helion gyromagnetic ratio $2 \mu'_h /\hbar$ (gas, sphere, 25 °C)	•	2.037 894 70(18)×10 ⁸	s ⁻¹ T ⁻¹	8.7×10 ⁻⁸
(gas, sphere, 25°C)	γ' _h	()	MHz T ⁻¹	8.7×10 ⁻⁸
	$\gamma_h'/2\pi$	32.434 1015(28) particle, α	MITIZ I	8./×10
ılpha particle mass	m_{α}	6.644 6565(11)×10 ⁻²⁷	kg	1.7×10 ⁻⁷
in u, $m_{\alpha} = A_{r}(\alpha)$ u (alpha particle rel. atomic mass times	· ·	4.001 506 179 149(56)	u	1.4×10 ⁻¹¹
energy equivalent	$m_{\alpha} c^2$	$5.971\ 9194(10)\times10^{-10}$	I	1.7×10 ⁻⁷
in MeV	m_{α}	3727.379 17(32)	MeV	8.6×10 ⁻⁸
alpha particle to electron mass ratio	m_{α}/m_{e}	7294.299 5363(32)	1110 1	4.4×10 ⁻¹⁰
lpha particle to proton mass ratio	$m_{\alpha}/m_{\rm e}$ $m_{\alpha}/m_{\rm p}$	3.972 599 689 07(52)		1.3×10 ⁻¹⁰
alpha particle to proton mass $N_{ m A} m_{lpha}$	$M_{\alpha}/M_{\rm p}$ $M(\alpha), M_{\alpha}$	$4.001\ 506\ 179\ 149(56)\times10^{-3}$	kg mol ⁻¹	1.4×10 ⁻¹¹
upim partiete motar mass πημέα		OCHEMICAL	Ag IIIOI	1.1/\10
Avogadro constant	$N_{\rm A}, L$	$6.022\ 1415(10)\times10^{23}$	mol ⁻¹	1.7×10 ⁻⁷
tomic mass constant	N/			
$m_{\rm u} = \frac{1}{12} m {\rm (}^{12}{\rm C}) = 1 \text{ u} = 10^{-3} \text{ kg mol}^{-1}/N_{\rm A}$	$m_{ m u}$	1.660 538 86(28)×10 ⁻²⁷	kg	1.7×10 ⁻⁷
energy equivalent	$m_{\rm u} c^2$	1.492 417 90(26)×10 ⁻¹⁰	J	1.7×10 ⁻⁷
in MeV		931.494 043(80)	MeV	8.6×10^{-8}
Faraday constant ⁸ N _A e	F	96 485.3383(83)	C mol ⁻¹	8.6×10 ⁻⁸
nolar Planck constant	$N_{\scriptscriptstyle{\mathrm{A}}} h$	$3.990\ 312\ 716(27)\times10^{-10}$	J s mol ⁻¹	6.7×10 ⁻⁹
	$N_{A}hc$	0.119 626 565 72(80)	J m mol ⁻¹	6.7×10 ⁻⁹
molar gas constant	R	8.314 472(15)	J mol ⁻¹ K ⁻¹	1.7×10 ⁻⁶
Soltzmann constant $R/N_{\rm A}$	k	1.380 6505(24)×10 ⁻²³	J K ⁻¹	1.8×10 ⁻⁶
in eV K ⁻¹		8.617 343(15)×10 ⁻⁵	eV K ⁻¹	1.8×10 ⁻⁶
	k/h	2.083 6644(36)×10 ¹⁰	Hz K ⁻¹	1.7×10 ⁻⁶
	k/hc	69.503 56(12)	$m^{-1} K^{-1}$	1.7×10 ⁻⁶
molar volume of ideal gas RT/p				
T = 273.15 K, p = 101.325 kPa	V_{m}	$22.413\ 996(39)\times10^{-3}$	m³ mol-1	1.7×10 ⁻⁶
Loschmidt constant $N_{\rm A}/V_{\rm m}$	n_0	$2.6867773(47)\times10^{25}$	m-3	1.8×10^{-6}
T = 273.15 K, p = 100 kPa	V_{m}	$22.710\ 981(40)\times10^{-3}$	$m^3 \text{ mol}^{-1}$	1.7×10^{-6}
Sackur–Tetrode constant (absolute entropy constant) ^h $\frac{5}{2}$ +ln[$(2\pi m_u k T_1/h^2)^{3/2} k T_1/p_0$]				
$T_1 = 1 \text{ K}, p_0 = 100 \text{ kPa}$	S_0 / R	-1.151 7047(44)		3.8×10 ⁻⁶
$T_1 = 1 \text{ K}, p_0 = 101.325 \text{ kPa}$	-	-1.164 8677(44)		3.8×10 ⁻⁶
tefan-Boltzmann constant $(\pi^2/60)k^4/\hbar^3c^2$	σ	5.670 400(40)×10 ⁻⁸	$W m^{-2} K^{-4}$	7.0×10 ⁻⁶
irst radiation constant $2\pi hc^2$	c_1	$3.74177138(64)\times10^{-16}$	$W m^2$	1.7×10 ⁻⁷
irst radiation constant for spectral radiance 2hc ²	c_{1L}	1.191 042 82(20)×10 ⁻¹⁶	$W m^2 sr^{-1}$	1.7×10 ⁻⁷
second radiation constant hc/k	c ₂	1.438 7752(25)×10 ⁻²	m K	1.7×10 ⁻⁶
Wien displacement law constant	4			
$b = \lambda_{\text{max}} T = c_2 / 4.965 \ 114 \ 231 \dots$	b	2.897 7685(51)×10 ⁻³	m K	1.7×10 ⁻⁶

^aSee the "Internationally Adopted Values" table for the conventional value for realizing representations of the volt using the Josephson effect.

See the "Internationally Adopted Values" table for the conventional value for realizing representations of the ohm using the quantum Hall effect.

CValue recommended by the Particle Data Group [Hagiwara et al., *Phys. Rev. D* **66**, 010001 (2002)].

dBased on the ratio of the masses of the W and Z bosons $m_{\mathbb{W}}/m_{\mathbb{Z}}$ recommended by the Particle Data Group [Hagiwara et al., *Phys. Rev. D* **66**, 010001 (2002)]. The value for $\sin^2\theta_{\mathbb{W}}$ they recommend, which is based on a particular variant of the modified minimal subtraction ($\overline{\mathbb{M}}$ S) scheme, is $\sin^2\hat{\theta}_{\mathbb{W}}/m_{\mathbb{Z}} = 0.23124(24)$.

^eThe helion, symbol h, is the nucleus of the ³He atom.

^fThis and all other values involving m_{τ} are based on the value of $m_{\tau}c^2$ in MeV recommended by the Particle Data Group [Hagiwara et al., *Phys. Rev. D* 66, 010001 (2002)], but with a standard uncertainty of 0.29 MeV rather than the quoted uncertainty of -0.26 MeV, +0.29 MeV.

gen summerical value of F to be used in coulometric chemical measurements is 96 485.336(16) $[1.7 \times 10^{-7}]$ when the relevant current is measured in terms of representations of the volt and ohm based on the Josephson and quantum Hall effects and the internationally adopted conventional values of the Josephson and von Klitzing constants K_{I-90} and R_{K-90} given in the "Internationally Adopted Values" table.

^hThe entropy of an ideal monoatomic gas of relative atomic mass A_r is given by $S = S_0 + \frac{3}{2}R \ln A_r - R \ln(p/p_0) + \frac{5}{2}R \ln(T/K)$.

Internationally Adopted Values of Various Quantities					
Quantity	Symbol	Value	Unit	Relative standard uncertainty u_r	
relative atomic mass of ^a ¹² C	$A_{r}(^{12}C)$	12		(exact)	
molar mass constant	$M_{_{11}}$	1×10 ⁻³	kg mol ⁻¹	(exact)	
molar mass of ¹² C	$M(^{12}C)$	12×10 ⁻³	kg mol⁻¹	(exact)	
conventional value of Josephson constant ^b	$K_{ m J-90}$	483 597.9	GHz V ⁻¹	(exact)	
conventional value of von Klitzing constant ^c	$R_{\kappa_{-90}}$	25 812.807	Ω	(exact)	
standard atmosphere	11 70	101 325	Pa	(exact)	
standard acceleration of gravity ^d	g _n	9.806 65	m s ⁻²	(exact)	

^aThe relative atomic mass $A_r(X)$ of particle X with mass m(X) is defined by $A_r(X) = m(X)/m_u$, where $m_u = m(^{12}C)/12 = M_u/N_A = 1$ u is the atomic mass constant, M_u is the molar mass constant, N_A is the Avogadro constant, and u is the unified atomic mass unit. Thus the mass of particle X is $m(X) = A_r(X)$ u and the molar mass of X is $M(X) = A_r(X)M_u$.

This the inotal mass constant, A_A is the Avogadro constant, and u is the difficult atomic mass diff. This the mass of particle X is $M(X) = A_r(X)M_u$.

This is the value adopted internationally for realizing representations of the volt using the Josephson effect.

This is the value adopted internationally for realizing representations of the ohm using the quantum Hall effect.

The value given was adopted by the 3rd General Conference on Weights and Measures (CGPM), 1903, and is the conventional value used to calculate the now

obsolete unit kilogram force.

COD	CODATA Recommended Values of Energy Equivalents – 2002							
	Relevant unit							
	J	kg	\mathbf{m}^{-1}	Hz				
1 J	(1 J) = 1 J	$(1 \text{ J})/c^2 =$ 1.112 650 056 ×10 ⁻¹⁷ kg	(1 J)/hc = 5.034 117 20(86)×10 ²⁴ m ⁻¹	(1 J)/b = 1.509 190 37(26)×10 ³³ Hz				
1 kg	$(1 \text{ kg})c^2 = 8.987 551 787 \dots \times 10^{16} \text{ J}$	(1 kg) = 1 kg	(1 kg)c/h = 4.524 438 91(77)×10 ⁴¹ m ⁻¹	$(1 \text{ kg})c^2/h =$ 1.356 392 66(23)×10 ⁵⁰ Hz				
1 m ⁻¹	$(1 \text{ m}^{-1})hc = 1.986 445 61(34) \times 10^{-25} \text{ J}$	$(1 \text{ m}^{-1})h/c=$ 2.210 218 81(38)×10 ⁻⁴² kg	$(1 \text{ m}^{-1}) = 1 \text{ m}^{-1}$	$(1 \text{ m}^{-1})c =$ 299 792 458 Hz				
1 Hz	$(1 \text{ Hz})h = 6.626 0693(11) \times 10^{-34} \text{ J}$	$(1 \text{ Hz})h/c^2 =$ 7.372 4964(13)×10 ⁻⁵¹ kg	$(1 \text{ Hz})/c=$ 3.335 640 951 $\times 10^{-9} \text{ m}^{-1}$	(1 Hz)= 1 Hz				
1 K	(1 K)k = 1.380 6505(24)×10 ⁻²³ J	$(1 \text{ K})k/c^2 =$ 1.536 1808(27)×10 ⁻⁴⁰ kg	(1 K)k/hc = 69.503 56(12) m ⁻¹	(1 K)k/h = 2.083 6644(36)×10 ¹⁰ Hz				
1 eV	(1 eV) = 1.602 176 53(14)×10 ⁻¹⁹ J	$(1 \text{ eV})/c^2 =$ 1.782 661 81(15)×10 ⁻³⁶ kg	(1 eV)/hc = 8.065 544 45(69)×10 ⁵ m ⁻¹	(1 eV)/h = 2.417 989 40(21)×10 ¹⁴ Hz				
1 u	$(1 \text{ u})c^2 =$ 1.492 417 90(26)×10 ⁻¹⁰ J	(1 u) = 1.660 538 86(28)×10 ⁻²⁷ kg	(1 u)c/h = 7.513 006 608(50)×10 ¹⁴ m ⁻¹	$(1 \text{ u})c^2/h =$ 2.252 342 718(15)×10 ²³ Hz				
1 E _h	$(1 E_h) = 4.35974417(75) \times 10^{-18} J$	$(1 E_h)/c^2 =$ 4.850 869 60(83)×10 ⁻³⁵ kg	$(1 E_h)/hc =$ 2.194 746 313 705(15)×10 ⁷ m ⁻¹	$(1 E_h)/h =$ 6.579 683 920 721(44)×10 ¹⁵ Hz				

		Relevant u	nit	
	K	eV	u	$E_{ m h}$
1 J	(1 J)/k = 7.242 963(13)×10 ²² K	$(1 \text{ J}) =$ $6.241 509 47(53) \times 10^{18} \text{ eV}$	$(1 \text{ J})/c^2 =$ 6.700 5361(11)×10 ⁹ u	(1 J)= 2.293 712 57(39) \times 10 ¹⁷ $E_{\rm h}$
1 kg	$(1 \text{ kg})c^2/k =$ 6.509 650(11)×10 ³⁹ K	$(1 \text{ kg})c^2 = 5.609 588 96(48) \times 10^{35} \text{ eV}$	$(1 \text{ kg}) =$ $6.022 \text{ 1415}(10) \times 10^{26} \text{ u}$	$(1 \text{ kg})c^2 =$ 2.061 486 05(35)×10 ³⁴ E_h
1 m ⁻¹	$(1 \text{ m}^{-1})hc/k =$ 1.438 7752(25)×10 ⁻² K	$(1 \text{ m}^{-1})hc = 1.239 \text{ 841 } 91(11) \times 10^{-6} \text{ eV}$	$(1 \text{ m}^{-1})h/c =$ 1.331 025 0506(89)×10 ⁻¹⁵ u	$(1 \text{ m}^{-1})hc =$ 4.556 335 252 760(30)×10 ⁻⁸ E_h
1 Hz	$(1 \text{ Hz})h/k = 4.799 2374(84) \times 10^{-11} \text{ K}$	$(1 \text{ Hz})h = 4.135 667 43(35) \times 10^{-15} \text{ eV}$	$(1 \text{ Hz})h/c^2 =$ 4.439 821 667(30)×10 ⁻²⁴ u	$(1 \text{ Hz})b = 1.519 829 846 006(10) \times 10^{-16} E$
1 K	(1 K)= 1 K	$(1 \text{ K})k = 8.617 \text{ 343}(15) \times 10^{-5} \text{ eV}$	$(1 \text{ K})k/c^2 =$ 9.251 098(16)×10 ⁻¹⁴ u	$(1 \text{ K})k = 3.166 \text{ 8153(55)} \times 10^{-6} E_{\text{h}}$
1 eV	(1 eV)/k = 1.160 4505(20)×10 ⁴ K	(1 eV)= 1 eV	(1 eV)/c ² = 1.073 544 171(92)×10 ⁻⁹ u	$(1 \text{ eV}) = 3.674 932 45(31) \times 10^{-2} E_h$
1 u	$(1 \text{ u})c^2/k =$ 1.080 9527(19)×10 ¹³ K	$(1 \text{ u})c^2 =$ 931.494 043(80)×10 ⁶ eV	(1 u) = 1 u	$(1 \text{ u})c^2 =$ 3.423 177 686(23)×10 ⁷ E_h
$1E_{ m h}$	$(1 E_h)/k =$ 3.157 7465(55)×10 ⁵ K	$(1 E_h) = 27.211 3845(23) \text{ eV}$	$(1 E_h)/c^2 =$ 2.921 262 323(19)×10 ⁻⁸ u	$(1 E_{h}) = 1 E_{h}$